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A method for the estimation of χ^1 torsion angles in proteins

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SUMMARY

A method for estimating α CH– β CH coupling constants from the shape and fine structure of NH– α CH fingerprint-region cross peaks of COSY spectra is presented. Spectral simulations have been used to analyse the effect of variations in ${}^{3}J_{NH-\alpha}$ CH, ${}^{3}J_{\alpha}$ CH- β CH, linewidths and digital resolution on the appearance of NH– α CH COSY cross peaks. On the basis of these simulations a set of rules for broadly categorising experimental NH– α CH cross peaks according to α CH– β CH coupling constants has been devised. The method has been applied to the analysis of NH– α CH cross peaks of hen lysozyme. The results are compared to previous measurements of α CH– β CH coupling constants using E.COSY techniques.

INTRODUCTION

Protein structures in solution are based on a large number of distance restraints derived from nuclear Overhauser enhancement (NOE) effects and on torsion-angle restraints derived from measured spin-spin coupling constants (Wüthrich, 1986). Restraints for the torsion angle χ^1 are based on measured ${}^{3}J_{\alpha CH-\beta CH}$ values and qualitative rather than quantitative information about these coupling constants is usually sufficient. For example, two measured $\alpha CH-\beta CH$ coupling constants of < 5 Hz correspond to $\chi^1 = +60^{\circ}$, whereas one large coupling constant (> 10 Hz) and one small coupling constant (< 5 Hz) correspond to $\chi^1 = -60^{\circ}$ or $\chi^1 = 180^{\circ}$; additional information about the relative intensities of the NH- βCH and $\alpha CH-\beta CH$ NOE effects is needed to distinguish between $\chi^1 = -60^{\circ}$ and $\chi^1 = 180^{\circ}$ (Wagner et al., 1987; Arseniev et al., 1988). Pairs of $\alpha CH-\beta CH$ coupling constants which differ by less than 5 Hz usually indicate side-chain averaging about χ^1 and are not, therefore, interpreted in terms of χ^1 angle restraints.

 α CH- β CH coupling constants, for residues with two β -protons, can be obtained from the relative displacements of cross-peak components in E.COSY and P.E.COSY spectra recorded in

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D₂O (Griesinger et al., 1987; Mueller, 1987). For threonine, isoleucine and valine residues, which contain only one β -proton, the α CH- β CH coupling constant must be measured from the antiphase splitting through α CH- β CH cross peaks of COSY spectra collected in D₂O and corrections for the distortions due to linewidth must be taken into account (Smith et al., 1991). Both of these methods for measuring α CH- β CH coupling constants suffer from limitations. The α CH- β CH region of E.COSY spectra is often very crowded and overlap of cross peaks can make accurate measurements of coupling constants impossible. Cross-peak intensity in COSY or E.COSY spectra can be very weak if the active α CH- β CH coupling constant is small; poor signal-to-noise ratios result in errors in the measured α CH- β CH coupling constants. The measurement of coupling constants is particularly difficult in the case where $\chi^1 = +60^\circ$ because both α CH- β CH cross peaks will be of low intensity.

In this paper an alternative method for the estimation of $\alpha CH-\beta CH$ coupling constants is presented. This method is based on analysis of the NH- αCH cross peak rather than the $\alpha CH-\beta CH$ cross peak. Use of the fingerprint region of the spectrum has the advantage of the good chemical-shift dispersion usually observed for the NH resonances. The analysis of the NH- αCH cross peaks presented here provides qualitative information about the $\alpha CH-\beta CH$ coupling constants which is useful for determining χ^1 angle restraints for structure calculations, for obtaining stereospecific assignments for βCH resonances in conjunction with NOE data, and for making assignments of cross peaks in the $\alpha CH-\beta CH$ region of the COSY spectrum. The method has been applied to the estimation of χ^1 values for hen egg-white lysozyme.

METHODS

Hen egg-white lysozyme was obtained from Sigma Chemical Company and dialysed at pH 3 to remove acetate. The protein was dissolved in 90% H₂O/10% D₂O at a concentration of 7 mM and at pH 3.8. Phase-sensitive COSY spectra were recorded at 55 °C on a home-built 500 MHz NMR spectrometer of the Oxford Centre for Molecular Sciences. The spectrometer is equipped with an Oxford Instrument Company magnet, a GE/Nicolet 1280 data acquisition system, a 293D pulse programmer and a Bruker probe. Data were processed using FTNMR and FELIX software (Hare Research Inc.) running on SUN computers of the Oxford Centre for Molecular Sciences. Standard phase-cycling schemes were used (Aue et al., 1976; Bax and Freeman, 1981). Phase discrimination in t_1 was achieved using the method of States et al. (1982). The transmitter frequency was set at the frequency of the water resonance and this resonance was suppressed by low-power, continuous wave irradiation during a 1-s preparation delay. 512 complex t_1 increments of 4096 complex points were collected. 32 transients were collected for each t_1 increment. Spectral widths of 5405 Hz were used. The spectra were resolution enhanced prior to Fourier transformation by double exponential multiplication (DM = 3.75) and trapezoidal multiplication (T1 = 256, T2 = 0) in the F₂ dimension and by trapezoidal multiplication (T1 = T2 = 128) in the F_1 dimension. After zero-filling once in the F_2 dimension and twice in the F_1 dimension the digital resolution was 0.66 Hz/point in F_2 and 2.6 Hz/point in F_1 . The horizontal axis is the F_2 dimension and the vertical axis is the F_1 dimension.

Peak-shape information was extracted from the experimental and simulated cross peaks as follows. A cross peak is selected in the spectrum. The contour scaling factor is set equal to the average peak height of the four antiphase components and the cross peak is plotted with four

contour levels. The contours are spaced logarithmically so that the nth level corresponds to an intensity of 0.7^n times the scaling factor; the four levels are drawn at 0.7, 0.49, 0.34 and 0.24 times the scaling factor. The peak shape is assessed quantitatively on the basis of two ratios, R_1 and R_2 , derived from the measurement of m, n, p and q as shown in Fig. 1a ($R_1 = m/n$, $R_2 = p/q$). The positions of the peak centres, required for the measurement of m and n, are interpolated by eye. The values of p and q are taken from the lowest plotted contour (corresponding to 0.24 times the



Fig. 1. Simulated NH- α CH cross peaks for residues with two β -protons. The horizontal axis represents F_2 (NH) and the vertical axis represents F_1 (α CH). All peaks were simulated with ${}^{3}J_{NH-\alpha}CH = 7.0$ Hz. The peaks in row (a) were simulated with linewidths of 7.5 Hz in F_1 and 5.5 Hz in F_1 , and with 512 t_1 values. The peaks in row (b) were simulated with linewidths of 7.5 Hz in F_2 and 5.5 Hz in F_1 , and with 512 t_1 values; the χ^1 values were averaged by +/-30° about the stated value. The peaks in row (c) were simulated with linewidths of 7.5 Hz in F_2 and 5.5 Hz in F_1 , and with 512 t_1 values; the χ^1 values were averaged by +/-30° about the stated value. The peaks in row (c) were simulated with linewidths of 7.5 Hz in F_2 and 5.5 Hz in F_1 , and with 256 t_1 values. The peaks in row (d) were simulated with linewidths of 15.5 Hz in F_1 and F_2 , and with 512 t_1 values. The two ratios R_1 and R_2 , used to measure overall peak shape and individual peak component shape, are defined as shown in the upper left-hand square: $R_1 = m/n$, $R_2 = p/q$.

peak height). In the case of experimental peaks the values of p and q are measured for all four cross-peak components and the values of m and n are measured twice. The outer cross-peak components are used for the measurement of m, n, p and q in the case of cross peaks with eight components. This procedure is repeated for each cross peak using the scaling factor appropriate for that peak.

 $NH-\alpha CH$ cross peaks were simulated by using the program SIMULATION (Redfield, unpublished data). The program assumes weak coupling and applies experimental parameters for digital resolution and resolution enhancement to antiphase cross peaks with Lorentzian lineshapes.

Coordinates for hen lysozyme were taken from the 2.0-Å resolution tetragonal type 2 crystal structure obtained by X-ray diffraction (Blake et al., 1967; Handoll, 1985) and from the 1.4-Å triclinic crystal structure obtained by neutron diffraction and provided by Dr. Sax Mason (Grenoble). Torsion angles are defined by the non-hydrogen atoms according to the IUPAC-IUB convention (1970). Coupling constants were computed using a Karplus equation (Karplus, 1959) with A, B and C values of 9.5, -1.6 and 1.8, respectively (DeMarco et al., 1978).

RESULTS AND DISCUSSION

A portion of the fingerprint region of the COSY spectrum of hen lysozyme is shown in Fig. 2a. Close inspection of this spectrum reveals that the NH– α CH cross peaks have a variety of shapes. For example, the peaks arising from D52 and Y53 have a pronounced rectangular shape whereas those arising from D66 and I78 have a squarer shape. This variation in cross-peak shape is very pronounced when 512 complex increments are collected in the t₁ dimension but is lost to a great extent when only 256 t₁ increments are collected as shown in Fig. 2b (Redfield, 1990). The cross-peak shape in the F₂ dimension is affected by the active NH– α CH coupling constant while the peak shape in F₁ is affected by both the active NH– α CH and passive α CH– β CH couplings. Thus, analysis of the fingerprint cross peaks may provide some information about the α CH– β CH coupling constants.

NH- α CH cross peaks have been simulated for various values of ${}^{3}J_{NH-\alpha CH}$ and ${}^{3}J_{\alpha CH-\beta CH}$ in order to understand the influence of these coupling constants on the observed NH- α CH crosspeak shapes; examples of these simulations are illustrated in Figs. 1 and 3. The overall peak shape and cross-peak component shape can be assessed quantitatively using the measurements shown in Fig. 1a; the overall peak shape is expressed by the ratio R_1 whereas the individual cross-peak component shape is expressed by R_2 . The ratios R_1 and R_2 , expected for various values of ${}^{3}J_{NH-\alpha CH}$ and ${}^{3}J_{\alpha CH-\beta CH}$, are summarised in Table 1. Several conclusions can be drawn from these simulations. The observed cross-peak shape is influenced strongly by the passive $\alpha CH-\beta CH$ coupling constants. A square peak shape is observed when the single α CH- β CH coupling or both α CH- β CH couplings are small. Thus, a square cross-peak shape is characteristic of a χ^1 angle close to 60° for residues with two β -protons, to a χ^1 angle close to 60° or 180° for threenines and isoleucines and to a χ^1 angle close to 60° or -60° for valines. This square shape is characterised by R_1 and R_2 values that are both less than 2.0. A rectangular cross peak is observed when one of the α CH- β CH coupling constants is large; that is, when the χ^1 angle is close to -60° or 180° for residues with two β -protons, close to -60° for threenines and isoleucines and close to 180° for valines. Rectangular cross peaks are often composed of eight components. However, the four



Fig. 2. Part of the fingerprint region of the phase-sensitive COSY spectrum of hen egg-white lysozyme collected with (a) 512 complex t_1 increments and (b) 256 complex t_1 increments.

central components may be of lower intensity than the outer components or altogether absent due to cancellation arising from a larger α CH linewidth or a small amount of averaging about χ^1 . The rectangular shape is characterised by R₁ values of more than 2.0 and R₂ values of less than 2.0. Cross peaks with a shape between square and rectangular are classified as intermediate; this shape arises when the α CH- β CH coupling constants are between 5 and 10 Hz and is characteristic of extensive motional averaging about χ^1 . The intermediate peaks can be distinguished from the square and rectangular ones on the basis of the shape of the individual cross-peak components. Cross-peak components have a more circular shape when the side chain is in a specific χ^1 conformation (60°, 180° or -60°), whereas the components are more elongated along F₁ when the coupling constants are averaged. The intermediate cross-peak shape is characterised by R₁ values between 1.5 and 3.0 and R₂ values greater than 2.0. Alanine residues, which contain three β -protons, give rise to NH- α CH cross peaks of intermediate shape similar to those obtained above for motional averaging about χ^1 .



Fig. 3. Simulated NH- α CH cross peaks for residues with one β -proton. The horizontal axis represents F₂ (NH) and the vertical axis represents F₁ (α CH). All peaks were simulated with ³J_{NH- α CH} = 7.0 Hz. The peaks in row (a) were simulated with linewidths of 7.5 Hz in F₂ and 5.5 Hz in F₁, and with 512 t₁ values. The peaks in row (b) were simulated with linewidths of 7.5 Hz in F₂ and 5.5 Hz in F₁, and with 512 t₁ values; the χ^1 values were averaged by +/-30° about the stated value.

A close inspection of the R₁ values listed in Table 1 shows that these depend on the value of ${}^{3}J_{NH-\alpha CH}$ as well as on ${}^{3}J_{\alpha CH-\beta CH}$; the value of R₁ decreases as ${}^{3}J_{NH-\alpha CH}$ increases. This arises because the splitting in F₂ is more sensitive to changes in ${}^{3}J_{NH-\alpha CH}$ than the splitting in F₁. The ratio R₂ is fairly insensitive to ${}^{3}J_{NH-\alpha CH}$ for all cross-peak types. The extent to which cross-peak shape information, in the form of the ratios R₁ and R₂, can be used to obtain χ^{1} information will depend on whether the value of the NH- α CH coupling constant is known. If ${}^{3}J_{NH-\alpha CH}$ has been measured then χ^{1} information can always be obtained from R₁ and R₂. If ${}^{3}J_{NH-\alpha CH}$ is not known then ambiguities may arise. For example, an R₁ value of 2.5 is characteristic of a rectangular peak when ${}^{3}J_{NH-\alpha CH}$ is large but is characteristic of an intermediate peak if ${}^{3}J_{NH-\alpha CH}$ is small. However, an R₁ value greater than 4.0 is always characteristic of a rectangular peak and indicates that ${}^{3}J_{NH-\alpha CH}$ must be small. A set of rules for classifying peaks as square, rectangular or intermediate on the basis of the R₁ and R₂ values is summarised in Table 2.

The effects of linewidth and digital resolution in F_1 on the observed peak shapes have also been investigated using simulations. Cross peaks simulated on the basis of 256 complex t_1 increments no longer have the characteristic shapes obtained using 512 t_1 increments as shown in Fig. 1c. They all have R_1 and R_2 values characteristic of the intermediate shape and cannot be used to obtain χ^1 information. Increasing the values of the NH and α CH linewidths also leads eventually to a loss of peak-shape definition. However, even with linewidths of about 15 Hz useful information about χ^1 can be obtained from the NH- α CH peak shape.

The fingerprint region of the COSY spectrum of hen lysozyme has been assigned fully (Redfield and Dobson, 1988). NH– α CH coupling constants have been measured for the majority of residues of lysozyme and α CH– β CH coupling constants are known for 57 residues (Smith et al.,

	$J_{N\alpha} = 4 Hz$		$J_{N\alpha} = 2$	/ Hz	$J_{N\alpha} = 1$	0 Hz
	R ₁	R ₂	R ₁	R ₂	Ri	R ₂
Two B-protons, 512 t, values.						
$LW(F_1) = 5.5 Hz, LW(F_2) = 7.5 Hz$						
$\gamma^1 = -60^\circ, 180^\circ; {}^3J_{\alpha\beta} = 3.4, 12.9 \text{ Hz}$	4.5	1.5	3.4	1.4	2.6	1.4
$\chi^1 = -60^\circ, 180^\circ + /-30^\circ; {}^3J_{\alpha\beta} = 5.0, 11.5 \text{ Hz}$	4.3	1.7	3.3	1.6	2.3	1.7
$\gamma^1 = +60^\circ$; ${}^{3}J_{\alpha\beta} = 3.4, 3.4 \text{ Hz}$	1.9	1.7	1.6	1.6	1.3	1.6
$\chi^{1} = +60^{\circ}, +/-30^{\circ}; {}^{3}J_{\alpha\beta} = 5.0, 5.0 \text{ Hz}$	2.3	1.9	1.8	1.8	1.3	1.8
χ^{1} = averaged; ${}^{3}J_{\alpha\beta} = 6.7, 6.7 \text{ Hz}$	2.5	2.5	2.1	2.2	1.6	2.1
χ^1 = averaged; ${}^3J_{\alpha\beta}$ = 5.7, 7.7 Hz	3.1	2.4	2.2	2.1	1.6	2.1
			$J_{N\alpha} = 2$	7 Hz		
			R,	R ₂		
Two β -protons, 256 t_1 values,						
$LW(F_1) = 5.5 Hz, LW(F_2) = 7.5 Hz$						
$\chi^1 = -60^\circ$, 180°; ³ J _{\alpha\beta} = 3.4, 12.9 Hz}			3.3	3.3		
$\chi^1 = +60^\circ; {}^3J_{\alpha\beta} = 3.4, 3.4 \text{ Hz}$			3.1	2.8		
χ^{1} = averaged; ${}^{3}J_{\alpha\beta}$ = 6.7, 6.7 Hz			2.9	2.8		
			$J_{N\alpha} = 1$	7 Hz		
			\mathbf{R}_1	\mathbf{R}_2		
Two β -protons, 512 t, values,						
$LW(F_1) = 15.5 Hz, LW(F_2) = 15.5 Hz$						
$\chi^1 = -60^\circ$, 180°; ${}^3J_{\alpha\beta} = 3.4$, 12.9 Hz			2.7	1.4		
$\chi^1 = +60^\circ; {}^3J_{\alpha\beta} = 3.4, 3.4 \text{ Hz}$			1.4	1.5		
χ^1 = averaged; ${}^3J_{\alpha\beta}$ = 6.7, 6.7 Hz			1.8	1.8		
	$J_{N\alpha} = $	4 Hz	$J_{N\alpha} = 7 Hz$		$J_{N\alpha} = 10 \text{ Hz}$	
	R ₁	R ₂	R	R_2	\mathbf{R}_1	R_2
One B-proton 512 t. values						
$LW(F_1) = 5.5 Hz, LW(F_2) = 7.5 Hz$						
$\gamma^{1} = +60^{\circ}.180^{\circ}(T.I); \ \gamma^{1} = +60^{\circ}60^{\circ}(V);$	4.4	1.4	3.3	1.3	2.5	1.4
$^{3}J_{cg} = 12.9 \text{ Hz}$						
$\gamma^{1} = +60^{\circ}.180^{\circ} + (-30^{\circ})^{\circ} = +60^{\circ}60^{\circ} + (-30^{\circ})^{\circ}$	4.3	1.4	3.1	1.4	2.3	1.4
$^{3}L_{e} = 11.5 \text{ Hz}$						
$\gamma^{1} = -60^{\circ}$ (T.I); $\gamma^{1} = 180^{\circ}$ (V); ${}^{3}J_{-9} = 3.4$ Hz	1.8	1.6	1.4	1.5	1.2	1.5
$\chi^{1} = -60^{\circ} + (-30^{\circ} (T, I); \chi^{1} = 180^{\circ} + (-30^{\circ} (V);$	2.0	1.7	1.6	1.6	1.2	1.6
${}^{3}J_{-9} = 5.0 \text{ Hz}$	2.0					
$\gamma^1 = \text{averaged}; {}^3J_{e^8} = 6.7 \text{ Hz}$	2.5	2.1	1.9	1.9	1.4	1.8
n						

TABLE 1 R_1 AND R_2 VALUES CALCULATED FOR VARIOUS TYPES OF NH– α CH CROSS PEAKS



Fig. 4. Examples of NH α CH cross peaks from the phase-sensitive COSY spectrum of hen lysozyme. The R₁ and R₂ values for these residues are listed in Table 4. On the basis of the peak-shape analysis, V2, L8, C80 and W111 are classified as rectangular, 178 and S81 as square, and A32, N44 and K97 as intermediate.

1991). The cross-peak ratios R_1 and R_2 have been measured for 103 of the 117 non-glycine residues of hen lysozyme and are summarised in Tables 3 and 4. Examples of these cross peaks are shown in Fig. 4. The cross peaks have been classified as square, rectangular, or intermediate according to the rules summarised in Table 2 using the values of R_1 , R_2 , and ${}^3J_{NH-\alpha CH}$. The χ^1 values derived from the peak-shape analysis are also summarised in Tables 3 and 4. For example, V2 has an R_1 value of 2.4 and an R_2 value of 1.6. Using the known NH- α CH coupling constant of 10.0 Hz this peak can be classified as rectangular indicating that V2 adopts a χ^1 value of about 180° in solution. N44, on the other hand, has an intermediate peak shape with R_1 , R_2 and

TABLE 2

RULES FOR CLASSIFYING CROSS PEAKS AS RECTANGULAR, SQUARE OR INTERMEDIATE ON THE BASIS OF R1, R2 AND ${}^{3}J_{NH-\alpha CH}$

	${}^{3}J_{N\alpha} = 2$	${}^{3}J_{N\alpha} = 4 \text{ Hz}$		${}^{3}J_{N\alpha} = 7 \text{ Hz}$		${}^{3}J_{N\alpha} = 10 \text{ Hz}$	
	R 1	R ₂	\mathbf{R}_1	R ₂	R ₁	R ₂	
Rectangular	≥ 3.5	≤ 1.8	≥ 2.5	≤ 1.8	≥ 2.0	≤ 1.8	
Square	≤ 2.3	≤ 1.8	≤ 1.8	≤ 1.8	≤ 1.5	≤ 1.8	
Intermediate	< 3.5	≥ 1.9	< 2.5	≥ 1.9	< 2.0	≥ 1.9	

TABLE 3 COMPARISON OF SIDE-CHAIN CONFORMATION DATA OBTAINED BY PEAK-SHAPE ANALYSIS AND E.COSY METHODS

		E.COSY m	ethods ^a	Peak-shape analysis					
Residue	$J_{N\alpha}$ (Hz) ^a	$J_{\alpha\beta(Hz)}{}^a$	χ^1 (°) ^a	Type ^b	R ₁	R ₂	χ ^t (°) ^c		
V 2	10.0	10.8	180	r	2.4	1.6	180		
F3	7.4	3.0/10.0	-60	r	2.7	1.5	-60/180		
C6	5.8	3.5/11.5	-60	r	3.5	1.3	-60/180		
E7	4.5	6.7/6.4	aver.	а	2.9	2.3	aver.		
K13	4.2	9.2/5.1	aver.	r	4.5	1.6	-60/180		
H15	9.2	2.6/11.2	-60	r	2.5	1.5	-60/180		
D18	5.7	11.0/4.2	180	r	3.5	2.1	-60/180		
N19	7.0	6.4/7.3	aver.	а	1.8	1.9	aver.		
Y20	5.5	2.3/11.7	180	r	3.2	1.7	-60/180		
Y23	8.6	10.9/2.7	-60	r	2.4	1.1	-60/180		
N27	5.4	10.3/2.4	-60	r	3.6	1.5	-60/180		
W28	6.0	10.7/4.1	-60/180	r	3.4	1.3	-60/180		
V29	5.9	11.1	180	r	2.8	1.4	180		
C30	3.8	10.8/5.3	180	r	4.5	1.6	-60/180		
F34	7.6	5.0/10.7	-60	r	2.8	1.5	-60/180		
N37	7.5	8.1/4.2	aver.	а	1.7	1.9	aver.		
N39	8.8	10.8/4.5	180	r	2.7	1.7	-60/180		
T40	5.4	4.5	60/180	s	1.4	1.4	60/180		
T43	9.3	3.7	60/180	s	1.2	1.4	60/180		
R45	7.7	6.9/6.7	aver.	a	2.0	2.1	aver.		
N46	8.8	4.7/11.2	-60	r	2.3	1.9	-60/180		
T47	4.4	2.6	60/180	s	1.6	1.4	60/180		
D48	7.7	2.6/3.7	60	s	1.5	1.5	60		
T51	9.8	9.3	-60	r	1.9	1.0	-60		
D52	9.6	11.6/3.6	-60	r	2.5	1.7	-60/180		
¥53	9.6	10.4/3.0	-60	r	2.3	1.5	-60/180		
R61	7.2	10.8/5.7	180	r	2.8	1.7	-60/180		
C64	8.8	2.7/4.6	60	s	1.2	1.0	60		
N65	9.4	11.4/4.5	-60/180	r	2.4	1.5	-60/180		
D66	10.0	5.0/4.5	60	s	1.2	1.2	60		
R68	9.7	4.8/6.5	aver.	a	1.5	1.9	aver.		
T69	9.3	9.3	-60	r	2.0	1.8	-60		
S72		5.4/7.6	aver.	а	2.6	3.1	aver.		
N74		10.5/3.9	-60/180	r	2.4	1.3	-60/180		
L75		12.4/2.1	-60	r	2.6	1.5	-60/180		
N77	7.4	8.3/5.9	aver.	а	1.9	2.2	aver.		
S85	5.8	5.7/7.4	aver.	а	2.0	1.6	aver.		
S86	5.8	6.4/4.1	aver.	а	1.9	1.9	aver.		
D87	8.9	11.5/5.1	180	r	2.0	1.2	-60/180		
I88	6.5	4.5	60/180	s	1.4	1.3	60/180		
T89		9.5	60	r	6.2	3.0	-60		
V92	5.6	10.1	180	r	2.7	1.5	180		
N93	4.4	10.8/3.5	-60/180	r	3.3	1.8	-60/180		
C94	6.3	4.0/12.2	180	r	3.2	1.4	60/180		

		E.COSY methods ^a		Peak-shape analysis					
Residue	$J_{Nlpha} \left(Hz\right)^a$	$J_{\alpha\beta(Hz)}{}^a$	χ^1 (°) ^a	Туреь	R ₁	R ₂	χ ¹ (°) ^c		
V99	5.2	6.3	aver.	a	2.0	1.9	aver.		
S100		7.7/4.0	aver.	а	1.6	1.6	aver.		
N101	7.0	6.6/5.6	aver.	а	1.7	1.9	aver.		
N106		10.5/3.6	-60/180	r	3.5	1.6	-60/180		
V109	4.0	8.0	aver.	а	2.6	2.4	aver.		
T118	9.8	4.2	60/180	s	1.1	1.5	60/180		
D119	6.7	11.7/4.9	180	r	3.5	1.4	-60/180		
W123	5.4	2.9/10.6	-60	r	3.7	1.4	-60/180		
I124	10.6	4.6	60/180	S	1.0	1.6	60/180		
R125	4.4	7.9/6.1	aver.	а	2.5	3.0	aver.		
C127	7.7	4.8/11.6	-60	r	2.8	1.6	-60/180		
R128	8.0	7.2/7.9	aver.	а	2.0	2.2	aver.		

TABLE 3 (continued	TA	B	LE	3	(contin	ued)
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^a Smith et al., 1991.

b r = rectangular cross peak; s = square cross peak; a = intermediate cross peak.

 $^{\circ}\chi^{1}$ classification based on peak-shape analysis.

TABLE 4 COMPARISON OF ADDITIONAL SIDE-CHAIN CONFORMATION DATA OBTAINED BY PEAK-SHAPE ANALYSIS WITH χ^1 VALUES IN THE CRYSTAL STRUCTURES OF HEN LYSOZYME

		Peak-shap	oe analysis			Crystal	
Residue	$J_{N\alpha}\left(Hz\right)^{a}$	Туреь	R ₁	R ₂	χ ¹ (°) ^c	χ^{I} (°) ^d	χ ¹ (°) ^e
R5		а	2.6	3.0	aver.	-176.4	170.9
L8	5.5	r	3.6	1.6	-60/180	178.3	-179.3
A9	3.7	a	2.5	2.2	alanine		
A10	3.9	a	2.5	2.3	alanine		
A11	4.8	а	2.4	2.2	alanine		
M12	4.6	r	3.6	1.4	-60/180	-82.6	-75.9
R14	4.4	а	2.8	2.4	aver.	-175.1	-77.6
L17	7.6	r	2.5	1.7	-60/180	-77.1	-73.3
R21	6.8	а	2.4	2.1	aver.	-80.1	-64.0
S24		S	1.4	1.9	60	76.2	62.1
A31	3.8	а	2.8	2.7	alanine		
A32	4.8	а	2.3	2.3	alanine		
K33	3.6	r	5.1	2.1	-60/180	171.4	166.8
E35	7.2	r	2.7	1.3	-60/180	-76.0	-72.7
S36	9.6	S	1.3	1.4	60	67.0	66.0
Q41	9.2	r	2.1	1.5	-60/180	-68.4	-68.0
A42	4.5	а	2.5	2.1	alanine		
N44	9.4	а	1.5	2.0	aver.	-73.0	176.3
S50	7.8	S	1.2	1.5	60	69.5	70.2
L56	9.7	r	2.0	1.5	-60/180	-73.3	-76.2

		Peak-shap	e analysis			Crystal	
Residue	$J_{N\alpha} (Hz)^{a}$	Туреь	R ₁	R ₂	χ ¹ (°) ^c	χ^1 (°) ^d	χ ¹ (°) ^ε
Q57	6.3	r	3.2	1.5	-60/180	-67.9	-64.6
158	8.0	r	2.5	1.4	-60	-70.5	-73.4
S60	5.1	S	1.5	1.4	60	72.4	59.0
178	8.0	S	1.1	1.2	60/180	-159.9	50.1
C80	3.6	r	3.7	1.4	-60/180	-62.4	-61.4
S81	3.6	S	1.8	1.5	60	59.6	59.8
A82	5.4	а	2.4	2.0	alanine		
L83	7.2	r	2.6	1.2	-60/180	-57.0	-58.7
L84	9.2	r	2.5	1.6	-60/180	-58.3	-64.2
A90	4.2	а	2.8	2.5	alanine		
K96	4.4	а	2.0	2.2	-60/180	-73.5	-67.0
K97	6.5	а	2.2	2.5	aver.	-97.2	173.6
198		r	2.6	1.5	-60	-60.3	-70.2
N103	8.2	a	1.7	2.0	aver.	-51.1	-61.7
M105	7.4	r	2.5	1.5	-60/180	-75.6	-65.6
A107	4.2	а	2.8	2.4	alanine		
W108	9.6	r	2.4	1.5	-60/180	-78.6	-71.1
W111	7.1	r	3.1	1.8	-60/180	178.1	179.3
R112	4.5	а	2.2	2.5	aver.	-171.8	-174.0
N113	5.8	а	1.7	1.9	aver.	-65.1	-73.1
R114	9.6	r	2.4	1.2	-60/180	-44.9	-53.0
C115	9.8	r	2.3	1.4	-60/180	-60.9	-58.5
K 116		r	3.3	1.9	-60/180	-166.7	-179.1
V120	4.6	S	1.6	1.5	180	-61.9	-66.6
Q121	5.0	a	2.4	2.9	aver.	~99.3	-72.7
A122	3.7	а	2.8	2.8	alanine		
L129	9.0	r	2.4	1.8	-60/180	-46.6	-74.4

TABLE 4	(continued)
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^a Smith et al., 1991.

^b r = rectangular cross peak; s = square cross peak; a = intermediate cross peak.

 $^{\rm c}\,\chi^{\rm I}$ classification based on peak-shape analysis.

^d 2.0-Å tetragonal structure (Handoll, 1985).

^e 1.4-Å triclinic structure (Mason, personal communication).

 ${}^{3}J_{NH-\alpha CH}$ values of 1.5, 2.0 and 9.4, respectively, indicating that the side chain is undergoing motional averaging about χ^{1} . All the alanine cross peaks give the expected intermediate peak shape. Using this approach χ^{1} information has been obtained for 93 of the possible 102 residues of hen lysozyme. Information for the nine remaining residues was not obtained either because of severe cross-peak overlap or because of very low cross-peak intensity.

 α CH- β CH coupling constants, measured from E.COSY experiments, have been reported for 57 residues in hen lysozyme (Smith et al., 1991). The side chains of 41 of these residues are predicted to be in one of the preferred staggered rotamers whereas the side chains of the remaining 16 residues are predicted to be undergoing motional averaging about χ^1 (Smith et al., 1991). The NH- α CH cross-peak fine structure could be analysed for 56 of these 57 residues and this



Fig. 5. Comparison of experimental (a) and simulated (b) NH- α CH cross peaks for six residues of hen lysozyme. The NH- α CH and α CH- β CH coupling constants used in the simulations are listed in Table 3. The NH linewidths used in the F₂ dimension were obtained from the NH- α CH coupling-constant fitting procedure (Smith et al., 1991). A linewidth of 5.5 Hz was used in the F₁ dimension.

analysis has predicted the same side-chain conformation for all but one of these residues. NH– α CH cross peaks simulated using the values of ${}^{3}J_{NH-\alpha CH}$ and ${}^{3}J_{\alpha CH-\beta CH}$ previously reported, are compared with the experimental cross peaks in Fig. 5; the agreement is striking. K13 is the only residue for which a different χ^{1} classification is obtained by the two methods. The NH– α CH cross-peak fine structure of K13 is distinctively rectangular (R₁ = 4.5 and R₂ = 1.6) but the difference in the two α CH– β CH coupling constants was found to be less than 5 Hz (9.2 Hz and 5.1 Hz) in the previous study (Smith et al., 1991). The NH– α CH cross peak of K13 was simulated using various values of ${}^{3}J_{\alpha CH-\beta CH}$ as shown in Fig. 6. The cross peak simulated with values of 9.2 and 5.1 Hz is very different in appearance to the experimental peak; this simulated peak gives R₁ and R₂ values of 3.5 and 2.4 which are characteristic of an intermediate peak. Better agreement



Fig. 6. (a) Experimental NH- α CH cross peak of K13. (b) NH- α CH cross peak simulated with ${}^{3}J_{\alpha CH-\beta CH} = 5.1$ and 9.2 Hz, the values measured from the E.COSY spectrum (Smith et al., 1991). (c) NH- α CH cross peak simulated with ${}^{3}J_{\alpha CH-\beta CH} = 5.0$ and 11.5 Hz.

is obtained with $\alpha CH-\beta CH$ coupling constants of 11.5 and 5.0 Hz. The close agreement between χ^1 classifications for 56 residues made using E.COSY methods and cross-peak shape analysis indicates that the latter is a reliable method for determining approximate χ^1 values in proteins.

 γ^{1} -angle information for an additional 37 residues has been obtained from the peak-shape analysis procedure. $\alpha CH-\beta CH$ coupling constants for these residues were not obtained previously from E.COSY methods because of the lack of firm β CH assignments or because of overlap in the E.COSY spectrum. The χ^1 -angle assignments for these residues are listed in Table 4. Of the 37 residues, 20 give rise to rectangular peaks, 7 to square peaks and 10 to intermediate peaks. In the previous study of side-chain conformation in hen lysozyme it was found that residues which adopt a single χ^1 value in solution are also found to have this value of χ^1 in the X-ray structure (Smith et al., 1991). The χ^1 values obtained from the 2.0-Å tetragonal and 1.4-Å triclinic structures of hen lysozyme are listed for the 37 residues in Table 4. All residues classified as square or rectangular on the basis of cross-peak analysis are found to have χ^1 values in both X-ray structures which are entirely consistent with the χ^1 classification from this analysis. In the earlier study of side-chain conformation it was also found that residues undergoing motional averaging about χ^1 in solution almost always have side chains which are on the surface of the protein with a high solvent accessibility (Smith et al., 1991). The 10 additional residues found in this study to have disordered side chains in solution are all located on the protein surface. It is interesting to note that three of the 10 residues are found to have different χ^1 values in the tetragonal and triclinic structures; a similar situation was observed for half of the residues undergoing motional averaging about χ^1 in the earlier study of hen lysozyme (Smith et al., 1991).

The peak-shape analysis method can also provide information that is useful at an early stage of the assignment task. For example, an NH- α CH cross peak belonging to an alanine must have an intermediate peak shape. A residue with two β -protons, giving rise to a square NH- α CH cross peak, would be expected to have a pair of very weak peaks in the α CH- β CH region of the COSY spectrum. A valine that shows a rectangular NH- α CH peak is more likely to give rise to a pair of strong α CH- γ CH₃ peaks in RELAY or HOHAHA spectra than a valine with a square NH- α CH peak.

The peak-shape analysis method for the qualitative assessment of χ^1 values should be applicable to proteins of up to at least 130 residues. Indeed, the characteristic peak shapes described here can be seen in published COSY spectra of acyl carrier protein and plastocyanin (Holak and Prestegard, 1986; Driscoll et al., 1987). If the protein of interest has linewidths that are significantly different from those used here for lysozyme or if the COSY spectrum was collected or processed with very different digital resolution or window functions, then cross peaks for the different χ^1 categories should be simulated using an appropriate set of parameters before the analysis is carried out.

CONCLUSION

A method, based on the analysis of NH– α CH cross-peak shapes, for obtaining qualitative information about χ^1 values has been presented. Cross peaks with a square or rectangular shape arise when a residue has a well-defined conformation about χ^1 . Ambiguities in the χ^1 classification (i.e. 180° versus -60°) can only be resolved on the basis of additional NOE information (Wagner et al., 1987; Arseniev et al., 1988). Cross peaks with an intermediate shape are characteristic of motional averaging about χ^1 . This type of qualitative information about χ^1 values is of use in the early stages of spectral assignment, in the stereospecific assignment of β -protons and in structure calculations. The method has been proven reliable using a group of 56 residues from hen lysozyme for which χ^1 information had been derived from earlier E.COSY measurements (Smith et al., 1991). In addition, χ^1 information has been obtained for another 37 residues of hen lysozyme.

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